

# Flat top energy stability at the LHC

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SPS Operation

- Beam energy : basic dependencies.
- Stability : expectations from magnets & experience from LEP & SPS.
- Absolute energy calibration.

More details and references to LEP work can be found in LHC Project note 334.

# Fundamentals I

- For a particle of charge  $Z$  in a planar ring, the momentum  $p$  is proportional to the magnetic field integral  $\oint B(s)ds$  ( $\perp$  to the machine plane) on the beam orbit :

$$p = \frac{Ze}{2\pi} \oint B(s)ds = Z \times 47.7 [\text{MeV}/c/\text{Tm}] \times \oint B(s)ds$$

- After all, accelerators are spectrometers with a limited ( $\sim$  permill) momentum acceptance !
- To understand how the beam energy varies, we must know how the fields sampled by the beam depend on time, on the machine state and on external conditions.

# Fundamentals II

The length of the beam orbit  $L$  is defined by the RF frequency  $f_{RF}$  because the RF frequency is an integer multiple  $h$  (harmonic number) of the revolution frequency  $f_{rev}$ :

$$f_{RF} = h f_{rev} = \frac{h \beta c}{L}$$

$\beta c$  is the speed of the particles. At the LHC,  $f_{RF} = 400.87$  MHz,  $h = 35640$ .

The beam momentum, RF frequency, orbit length, machine circumference and magnetic field integral are correlated.

# Magnetic fields

The contributions to the field integral (and therefore to the momentum) can be roughly split into three components :

$$p = p_d + p_Q + p_\varepsilon$$

with contributions :

Typical contribution

- $p_d$  from dipole magnets  $\geq 99.8\%$
- $p_Q$  from quadrupole magnets  $\leq 1\text{-}2 \text{ permill}$
- $p_\varepsilon$  from higher order fields, orbit correctors...  $\sim 10^{-4} \text{ or less}$

# Dipoles Dominate

- By 'construction' the main dipoles define the energy → largest contribution to p.
- The **absolute field** is expected to be known to  $\sim 0.1\%$  from the SM18 magnet measurements. For comparison :
  - LEP  $\sim 0.1\%$
  - SPS  $\sim 0.2\%$
- The **reproducibility** of the dipoles is expected to be **better than  $10^{-4}$**  . For comparison :
  - LEP  $\leq 10^{-4}$  (despite abnormal temperature sensitivity and vagabond DC currents from trains)
  - SPS  $\leq 4 \times 10^{-5}$  (knowledge limited by accuracy of instruments)
- Note that a good field reproducibility is only achieved with a correct and reproducible magnet cycling (between fills).

# Quadrupoles matter !

- **Quadrupoles** are interleaved with the dipole to focus the beam. Their  $B(s)$  field is proportional to the distance to the magnet axis.
- Ideally the beam is centered on the axis of every quadrupole → no net field ! In a real machine it can only be centered on average.
- The contribution of the quadrupoles depends on  $L$  ( $\Leftrightarrow$  defines how far away the beam is on average from the quad. axis) and on a property of the optics, the momentum compaction factor  $\alpha$  :

$$\frac{dP_Q}{P} = -\frac{1}{\alpha} \frac{L - L_c}{L_c} \cong -3030 \frac{L - L_c}{L_c}$$

$L$  = actual orbit length

$L_c$  = central orbit length  $\Leftrightarrow$  beam centered on average in the quadrupoles - defines the machine circumference !

Large enhancement !!!

Example :  $\frac{dP_Q}{P} = 10^{-4} \Rightarrow \frac{L - L_c}{L_c} \cong 3 \cdot 10^{-8} \Rightarrow L - L_c = 0.9 \text{ mm}$

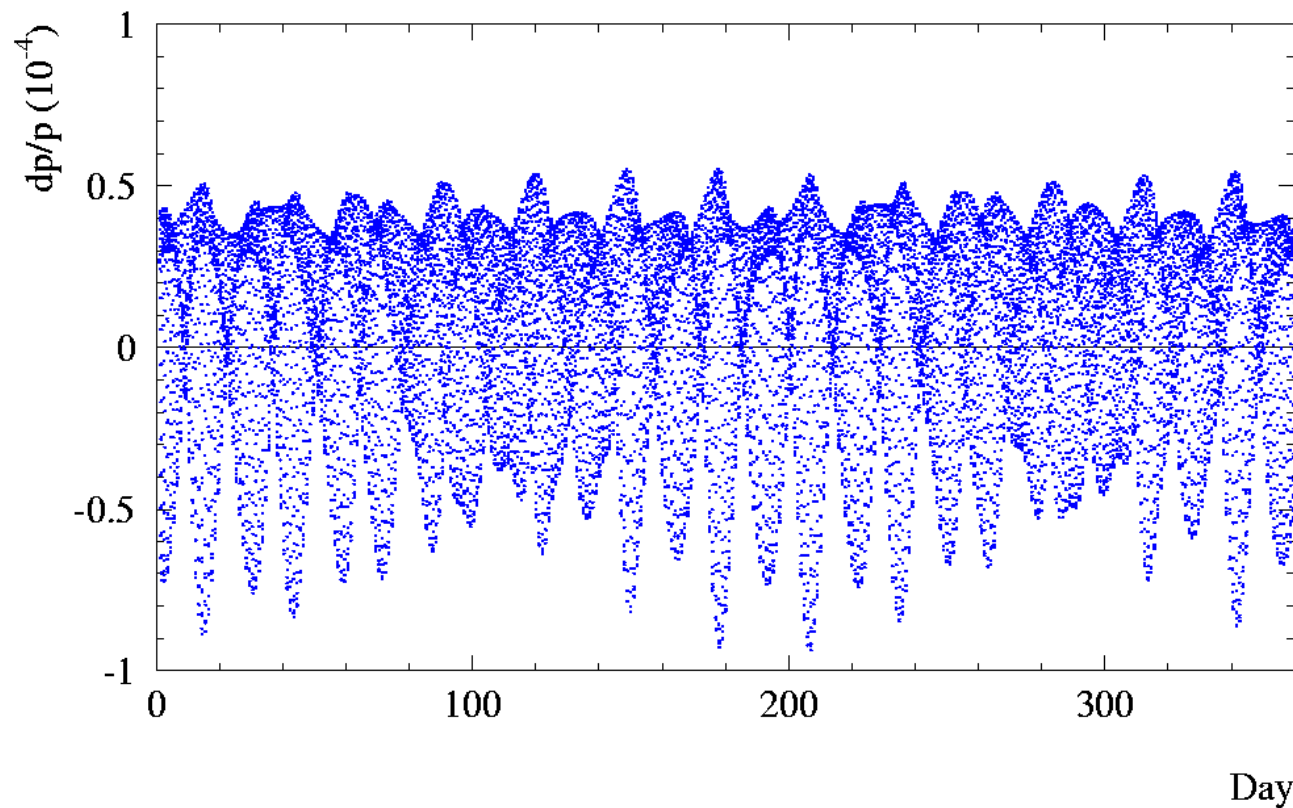
# RF frequency again...

- Remember that  $L$  is defined by the RF frequency and ideally  $L = L_c$ . A change of RF frequency (at fixed dipole field !) leads to a change of energy via the fields of the quadrupoles.
- The RF frequency corresponding to  $L_c$  is called the central RF frequency. The measurement of  $L_c$  is not very difficult ... but beware of systematic errors ! Relative measurements can be very accurate !
- By symmetry the energy changes also when the circumference changes !!

# Earth tides in 2007-2008...

Earth tides provoke elastic deformations of the crust that change the machine circumference and therefore  $L_c$ . They affected the LEP beam energy, and the LHC will feel them too !

Below is the predicted energy shift due to tides from 01 June 2007 – 31 May 2008

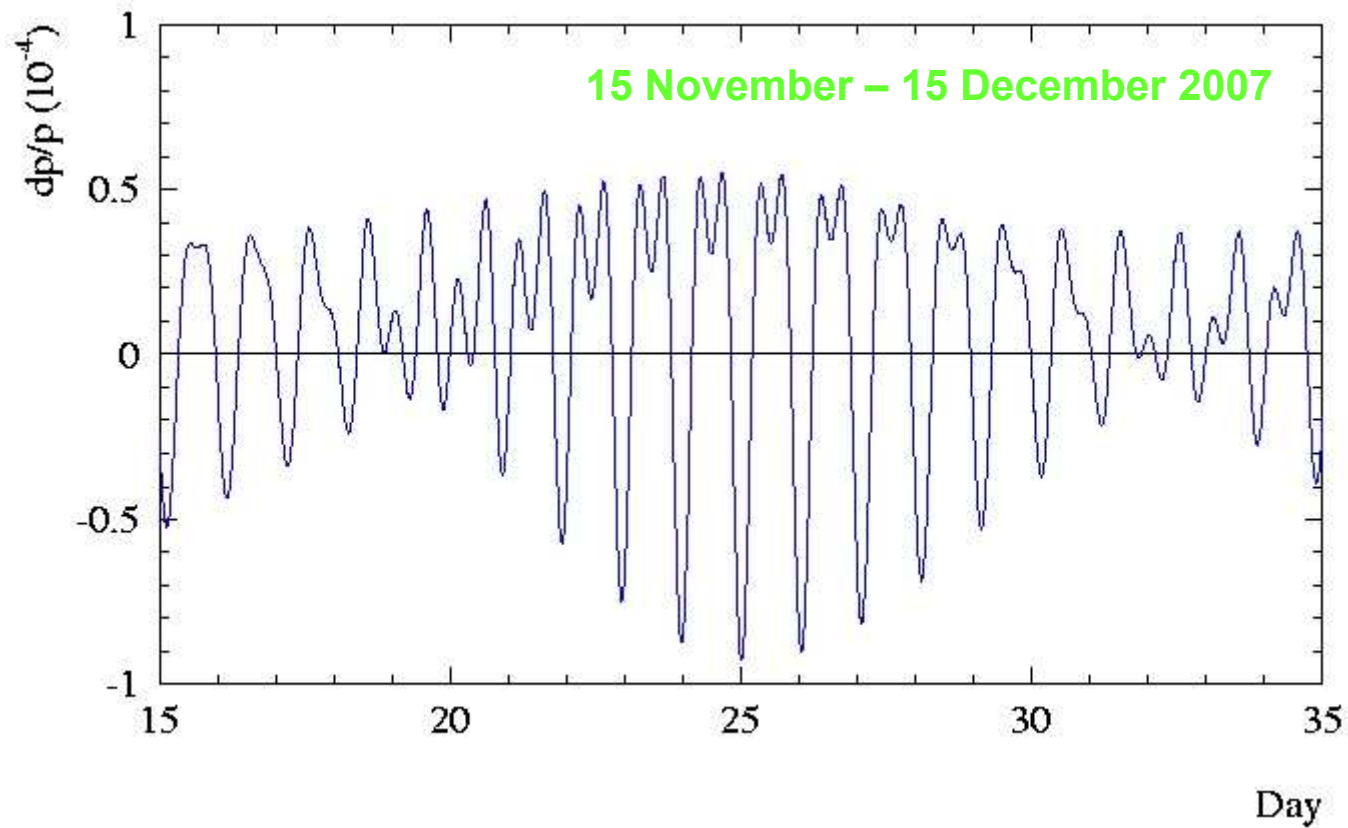


The accuracy of the prediction is at the level of a few % (from LEP data).



# Tides in more details

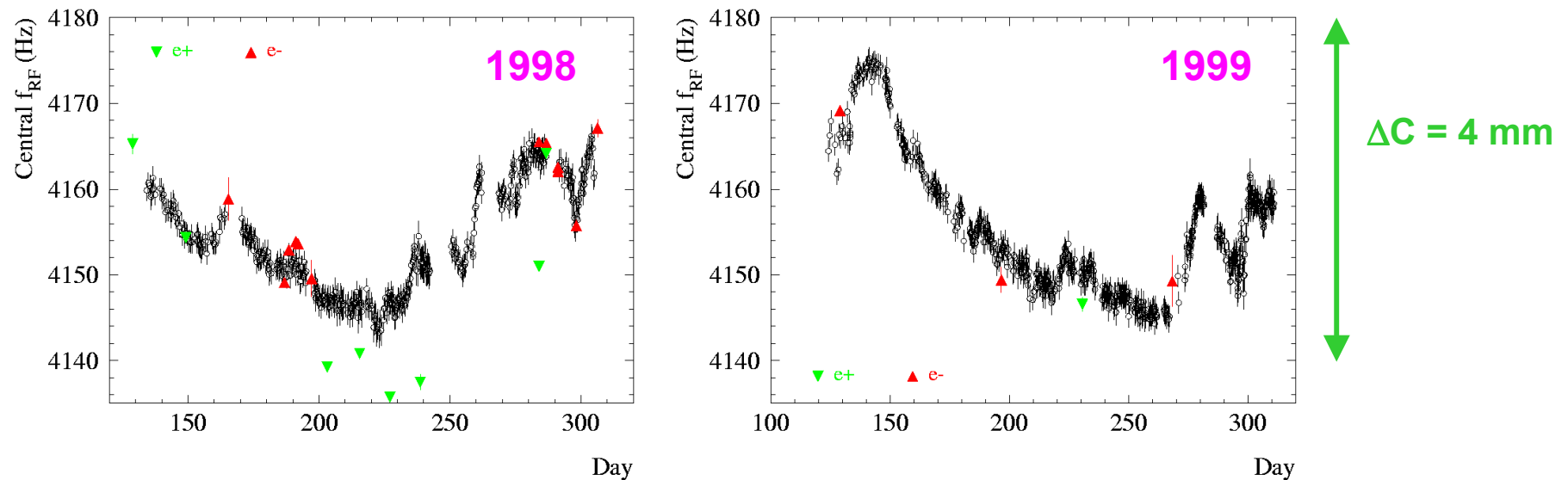
Tide details for November-December 2007



# LEP (LHC) circumference

- The LEP ring was also subject to large (but slow)  $L_c$  changes over a run. Beam position monitors and dedicated central RF frequency measurements (for absolute calibration) were used to track changes.
- A similar exercise will have to (and can be) made at the LHC !

Example of the long term evolution of the LEP circumference (here the last 4 digits of the central frequency of 352 MHz) – corrected for tidal effects :



# Other contributions...

- **Higher order fields** (mainly sextupole) can also contribute to the energy when the beam orbit is not well corrected. For the LHC I expect this effect to be **negligible ( $\approx 10^{-5}$ )**, as it was for LEP, because the orbit must be extremely well controlled (feedback).
- **Orbit correctors** (small dipole used to correct the beam orbit – mainly to counteract the quadrupole misalignment) **can affect the momentum when they are powered systematically with the same sign.**
  - A careful orbit correction can prevent / limit energy changes from this source to  $\leq 10^{-4}$ . It is also possible to correct for it – as was done for LEP energy calibration.
  - Note that sometimes orbit correctors are used on purpose to change p :
    - Orbit correctors were used at LEP to boost the energy.
    - Orbit correctors will be used during LHC injection to stabilize the LHC momentum wrt the SPS.

# Summary on stability and accuracy

| Contribution | Absolute calibration :<br>rel. accuracy ( $10^{-4}$ ) | Stability ( $10^{-4}$ ) |
|--------------|---|-------------------------|
| Dipoles      | $\approx 7$   | $< 1$                   |
| Quadrupoles  | $\approx 2$   | 4-5                     |
| Others       | $< 1$   | $< 1$                   |

- The momentum is expected to vary by :
  - $4-5 \times 10^{-4}$  over a year
  - $1-2 \times 10^{-4}$  over 24 hours
- The variations are driven mostly by circumference changes that can be measured / predicted to  $< 5 \times 10^{-5}$  (or better). We can build on the LEP experience !

# Absolute energy calibration

At LEP energy calibration was based 2 important ingredients :

- The beams could polarize spontaneously in favourable conditions (a consequence of synchrotron radiation).
- The spin precession frequency is proportional to  $\oint B(s)ds$  and therefore to  $p$ .

→ resonant depolarization to determine the energy from the spin precession frequency.

To use a similar method at the LHC would require polarized protons – not really in the baseline !

We must turn to other methods...

## Ions ...

- It is possible to determine the machine circumference  $L_c$  and absolute proton momentum  $p$  at the same time from a measurement of the difference in revolution frequency of a proton and 'ion' beam (i.e. the difference of speed !):

$$P \cong m^p c \sqrt{\frac{f_{RFc}^p}{2(f_{RFc}^p - f_{RFc}^i)} (\mu^2 - 1)}$$

$$\mu = \frac{m^i}{Z m^p}$$

$f_{RFc}$  = central RF freq.

( $p$  = proton,  $i$  = ion)

- This technique was already used at LEP ( $e^+ / p$ ) and SPS ( $p / Pb$ ).
- The tricky bit** : the machine state must be identical (fields, orbit length...) for the two beams or the differences must be known precisely !

## SPS Example : p / Pb

At the end of 2002, the last SPS Pb beams before the LHC area were used to perform a calibration of the SPS at 450 GeV/c. To enhance the accuracy,  $\text{Pb}^{53+}$  was used instead of fully stripped  $\text{Pb}^{82+}$ .

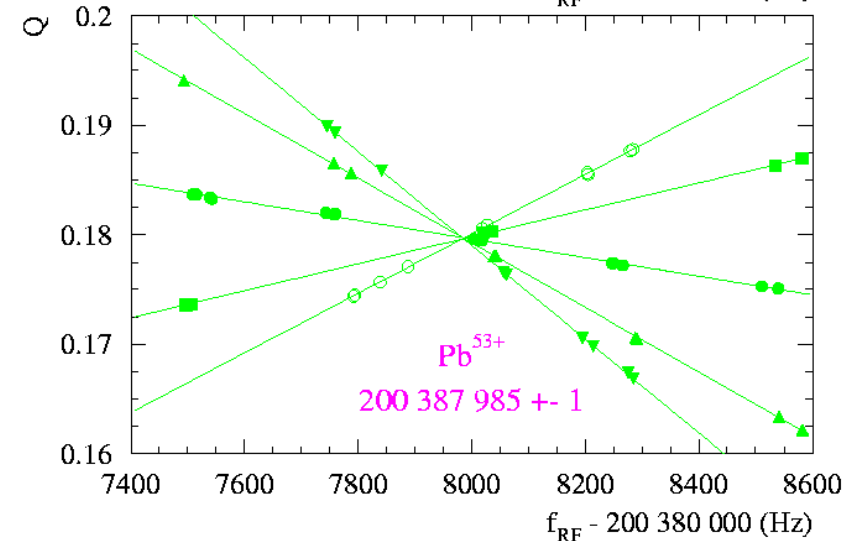
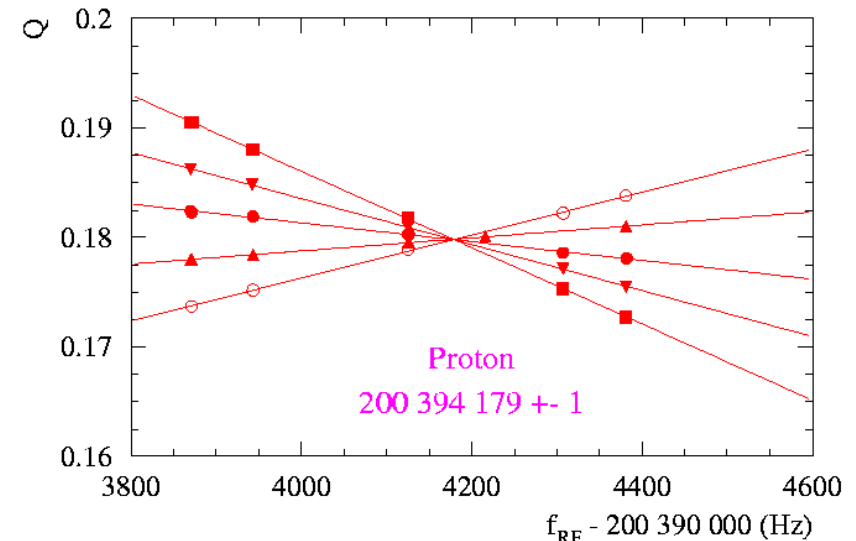
Frequency difference  $\text{Pb}^{53+}$ -p :

$\Delta f = 6.2 \text{ kHz}$  (with an error of  $\sim 2 \text{ Hz}$ )

SPS proton momentum at 450 GeV/c :

$$p = 449.18 \pm 0.14 \text{ GeV/c}$$

i.e. an accuracy of  $3 \times 10^{-4}$ .

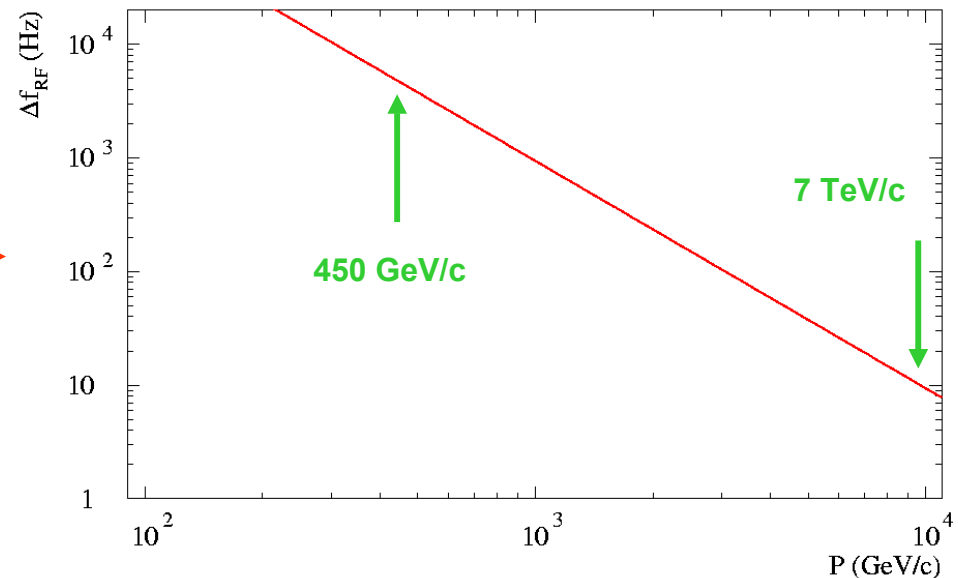


# Ions at the LHC

- The 'problem' with ions at the LHC is the small difference they exhibit as compared to protons. RF frequency differences scale with  $1/p^2$  (so does the difference in speed !!).
- At 7 TeV/c requirements on measurement accuracy and machine stability (fields & L) seem beyond any hope !
- A reasonable calibration may be obtained up to  $\sim 1$  TeV/c.

RF frequency difference between protons and Pb ions versus momentum :

- $\Delta f \sim 20$  Hz at 7 TeV/c
- Accuracy  $\sim 0.5$ -1 Hz (LEP best !)





# A spectrometer

- One (of three) energy calibration methods for LEP200 where resonant depolarization did not work (no polarization ...) was based on a **spectrometer magnet** :
  - A special dipole magnet calibrated to an accuracy of  $\sim \text{few } 10^{-5}$  and heavily instrumented with temperature and field probes.
  - The dipole was surrounded by  $\sim 15$  m long field and magnet free region equipped with high precision beam position monitors ( $O(\mu\text{m})$ ) to measure the beam angle through the spectrometer dipole.
  - With this device the calibrations performed at 45 GeV using resonant depolarization were extrapolated to 100 GeV with an accuracy of  $\sim 10^{-4}$ .
- A priori such concept could work at the LHC. Some issues :
  - Longer lever arm for extrapolation (0.45-1 TeV/c  $\rightarrow$  7 TeV/c).
  - Space !!!!!!!

# Summary

- At the LHC the momentum at flat top is expected to vary by :
  - $4\text{-}5 \times 10^{-4}$  over a year
  - $1\text{-}2 \times 10^{-4}$  over 24 hours
  - The variations are driven mostly by circumference changes.
- The absolute p is expected to be known to slightly better than 0.1%.
- The dominant error on the absolute momentum is coming from the knowledge of the dipoles.
- Absolute calibrations using Pb ions can give accuracies of  $\sim \text{few} \times 10^{-4}$  up to  $\sim 1 \text{ TeV}/c$  : provides a cross-check of the dipoles at low(er) field...
- Absolute p calibrations at  $7 \text{ TeV}/c$  to  $\sim 10^{-4}$  require new (and delicate) spectrometers, polarized protons (?), other ideas....